

MODEL OF DYNAMIC INTEGRATED INVENTORY AND DISTRIBUTION PROBLEM FOR GASOLINE SUPPLY CHAINS



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TDLog

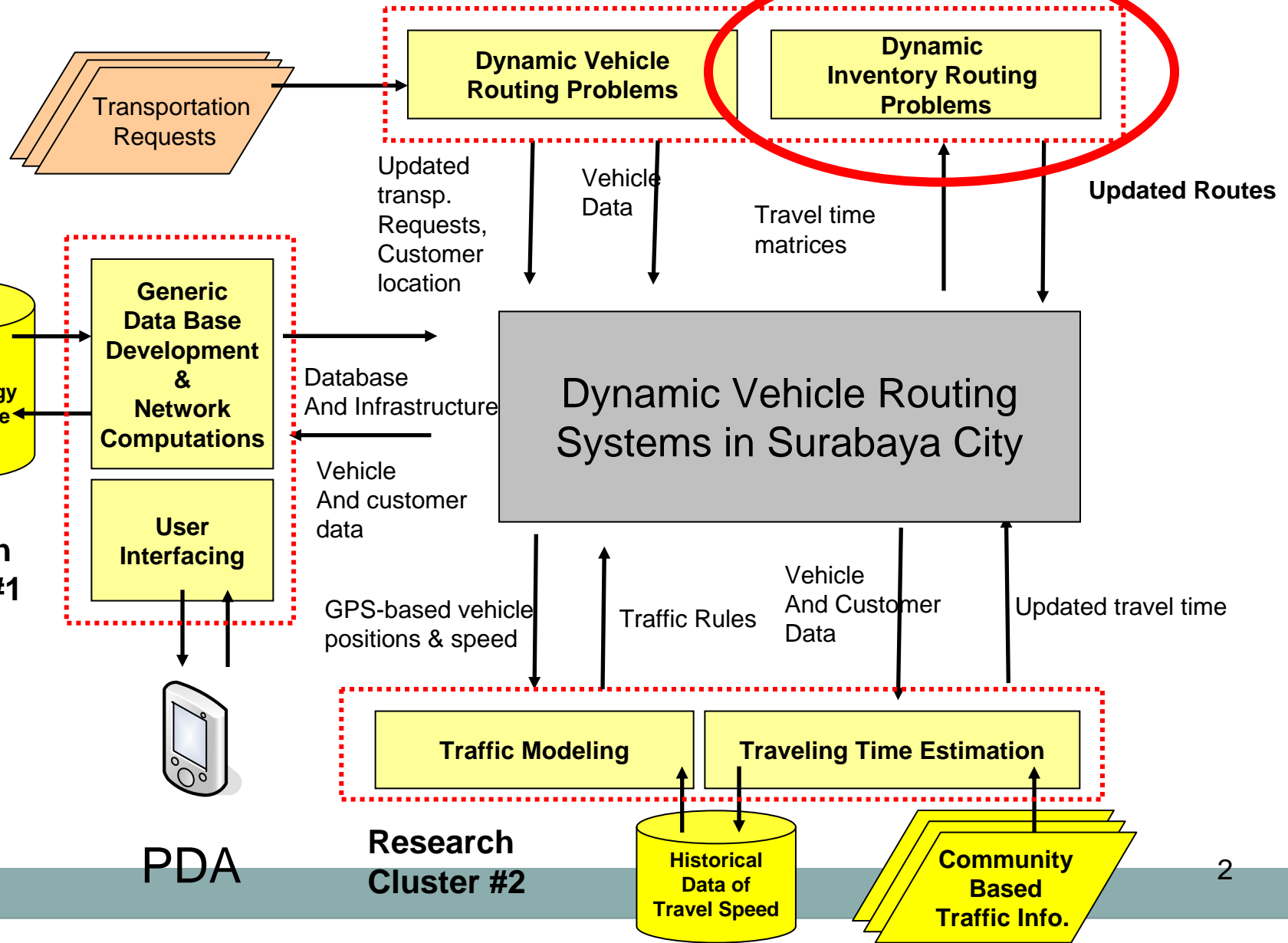


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Collaboration Research

Research Cluster #3



Background



Modern economy markets tend to become increasingly open and competitive

Companies now need to focus on **timeliness** to ensure not only their competitiveness, but also their survival.

Efficient, just-in-time, distribution systems where goods are delivered at the right place, in the right quantity and exactly when needed

Strategic Alliances

The objective of supply chains is to minimize system wide costs and increase efficiency while satisfying service level requirements

One of SC initiatives is to build *strategic alliances* within supply chain players.

Retailer-Suppliers Partnerships (RSP)

Quick
Response (QR)

Continuous
Replenishment
(CR)

Vendor
Managed
Inventory (VMI)

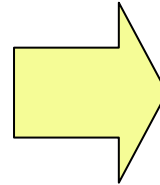
VMI : definition



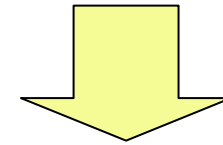
VMI : the needs of integrated decisions

Under VMI system, the supplier can :

- decide which retailers should be replenished at which times, and with how much product.
- coordinate the deliveries to the retailers



An operational-level decision tool to assist the coordination of inventory management and distribution decision



**Integrated
Inventory and Distribution
Decisions**

Gasoline Supply Chains



Gasoline Stations either owned By PERTAMINA, a SOE, or its partners



Depot



Existing Vs Proposed System



Existing

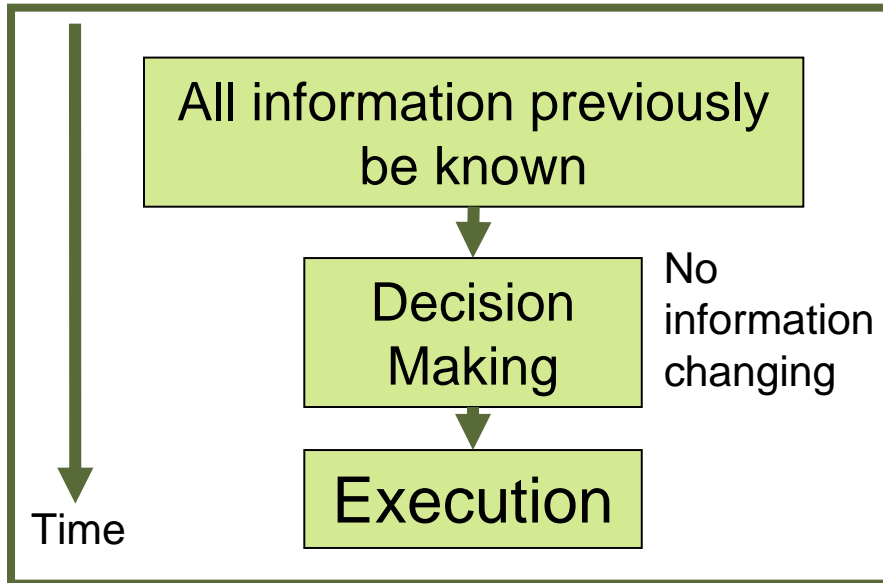
- The retailer (“gasoline stations”) orders fuels from the supplier/depot (“Pertamina”)
- The supplier collects orders from many stations and then solves the routing problem over the stations who ordered.
- The current system may produce an “unfair” allocation of gasoline (a limited supply !) among the stations, since the supplier have no information about the inventory level of each station.

Proposed

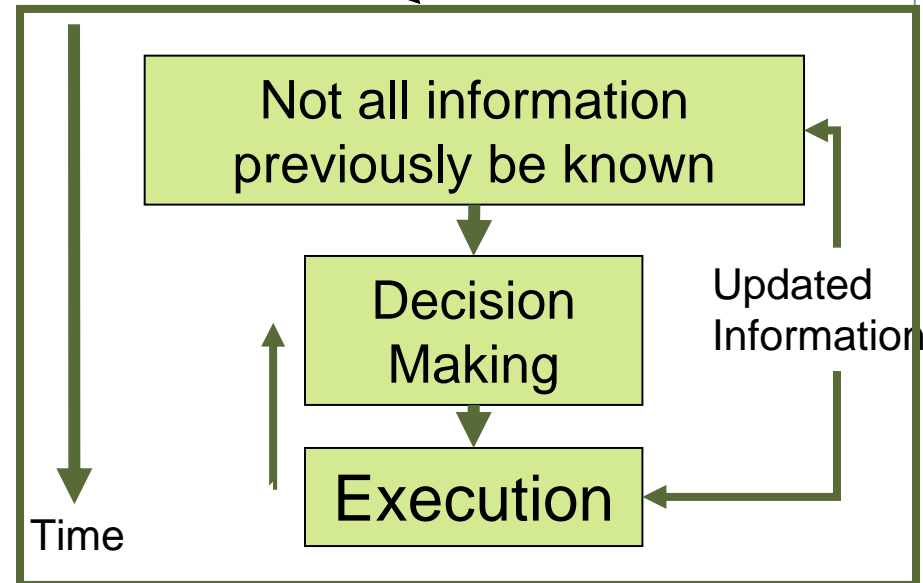
- The supplier takes both inventory decisions and routing decisions.
- The supplier is responsible to decide when and how much of replenishment and ensure that there would be no stockouts.
- The replenishment based on the realtime inventory level of stations.

Problem Background

Static IIDP



In fact...



-Federgruen dan Zipkin (1984) → one period

-Abdelmaguid and Dessouky (2004, 2006) → multiperiod

-Campbell et.al (1998)

- Not commonly discussed

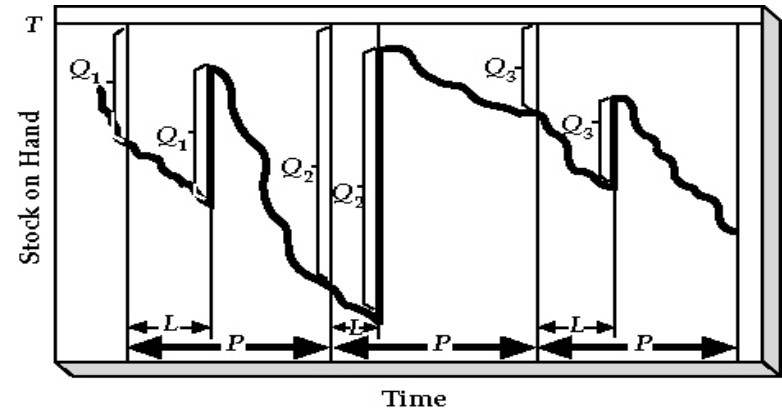
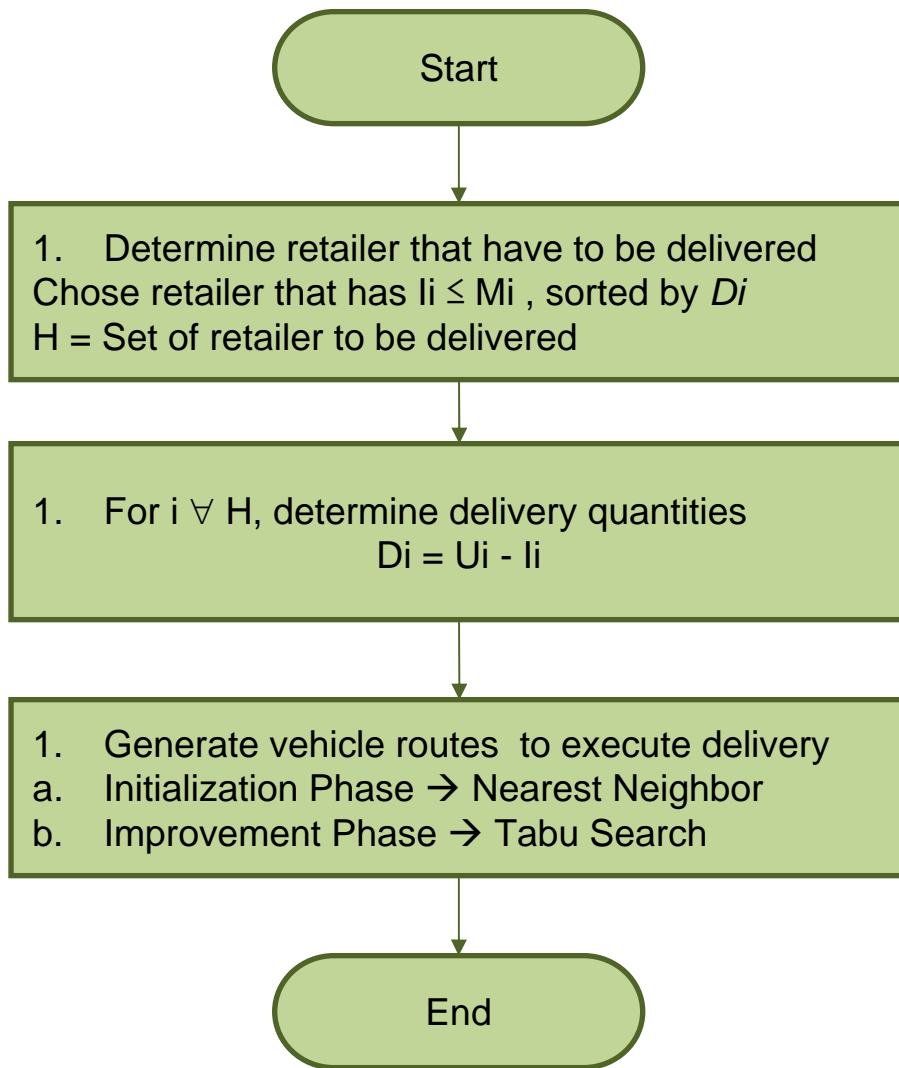
Model Formulation for Static IIDP

Based on models of Abdelmaguid (2004) and Campbell (1998)

- Mathematical Model:

<p><i>Min</i></p> <p>Subject to:</p> $\sum_{v=1}^V f_t x_{ojv} + \sum_{i=0}^N \sum_{j=0}^N \sum_{v=1}^V c_{ij} x_{ijv}$	<p>Minimization of Transportation Costs (Fixed and Variable)</p>	
$\sum_{\substack{j=0 \\ j \neq i}}^N x_{ijv} \leq 1$ $\sum_{\substack{k=0 \\ k \neq i}}^N x_{ikv} - \sum_{\substack{l=0 \\ l \neq i}}^N x_{liv} = 0$	<p>$i = 0, \dots, N; v = 1, \dots, V(1)$</p> <p>$i = 0, \dots, N; v = 1, \dots, V(2)$</p>	<p>} Route synchronization</p>
$y_{ijv} - q_v x_{ijv} \leq 0$	<p>$i = 0, \dots, N; j = 0, \dots, N; i \neq j; v = 1, \dots, V(3)$</p>	<p>Vehicle Capacity</p>
$\sum_{\substack{k=0 \\ k \neq i}}^N y_{ikv} - \sum_{\substack{l=0 \\ l \neq i}}^N y_{liv} \leq 0$	<p>$i = 1, \dots, N; v = 1, \dots, V(4)$</p>	<p>Subtour elimination</p>
$L_i + \sum_{v=1}^V \left(\sum_{\substack{l=0 \\ l \neq i}}^N y_{liv} - \sum_{\substack{k=0 \\ k \neq i}}^N y_{ikv} \right) \leq D_i$	<p>$i = 0, \dots, N; v = 1, \dots, V(5)$</p>	<p>Lower bound constraint</p>
$D_i \leq \sum_{v=1}^V \left(\sum_{\substack{l=0 \\ l \neq i}}^N y_{liv} - \sum_{\substack{k=0 \\ k \neq i}}^N y_{ikv} \right) + U_i$	<p>$i = 0, \dots, N; v = 1, \dots, V(6)$</p>	<p>Upper bound constraint</p>
$y_{ijv} \geq 0$	<p>$i = 0, \dots, N; j = 0, \dots, N; i \neq j; v = 1, \dots, V(7)$</p>	<p>} Non negativity constraint</p>
$x_{ijv} = 0$	<p>$i = 0, \dots, N; j = 0, \dots, N; i \neq j; v = 1, \dots, V(8)$</p>	<p>} Binary variable</p>

Heuristic : Static IIDP



Notes:

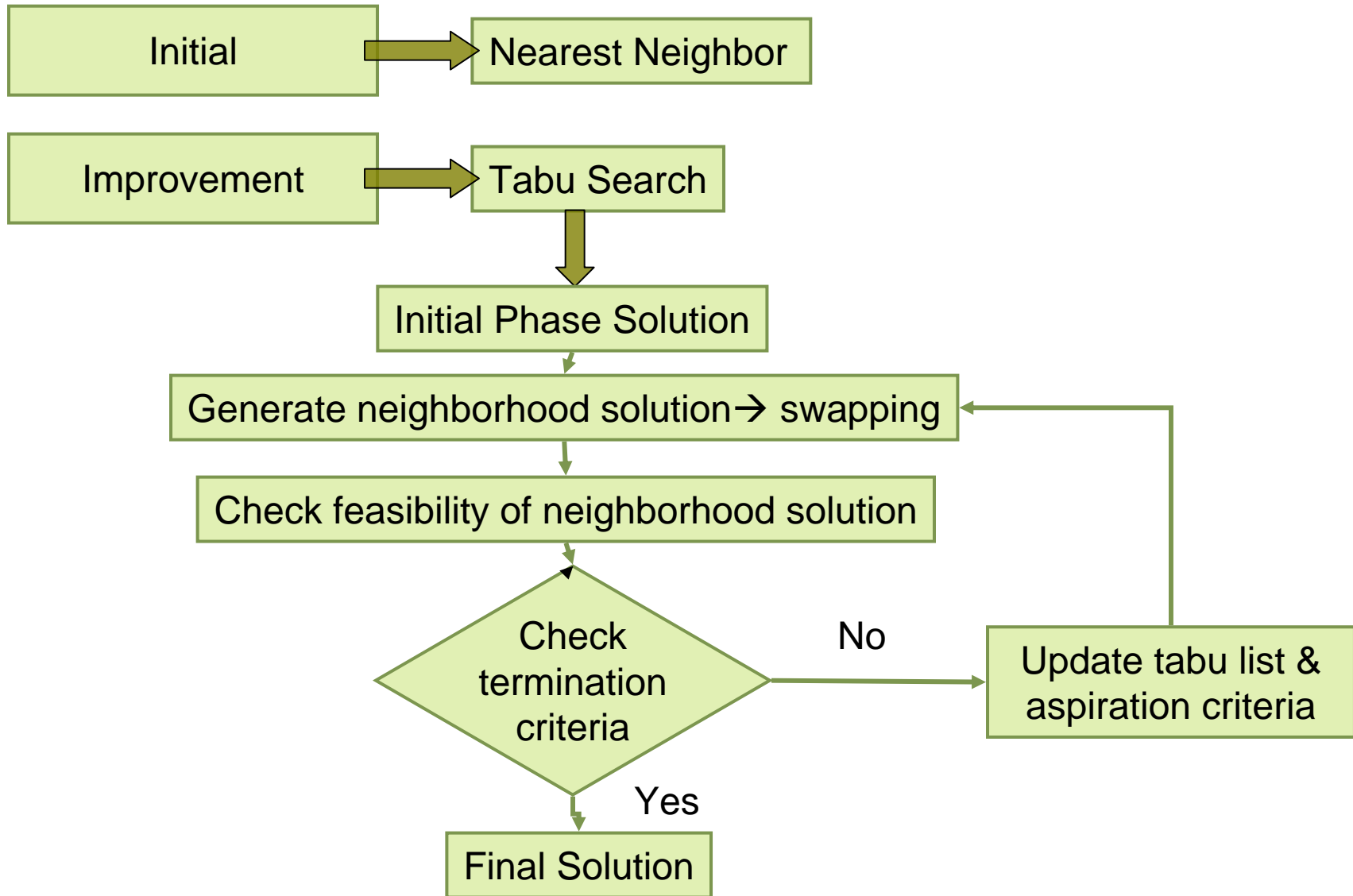
l_i = Inventory level at the time review

M_i = Minimum inventory level to be maintained

U_i = Maximum inventory level

D_i = Product volume to be delivered

Static IIDP: Generating Vehicle Routes



Inventory Level

Reorder Point

$$ROP_i = (D_i \times LT) + (Z \times \text{St.Dev} \times \sqrt{LT})$$

Dimana:

ROP_i = Reorder Point of station i

D_i = *Throughput* per hour of station i

LT = *lead time duration* (=4 hours)

Z = Z value of determined Service Level (*service level* 95%, $Z= 1.645$)

Upper Bound of Inventory Point

$$U_i = (D_i \times T) + (Z \times \text{StDev} \times \sqrt{LT})$$

Dimana:

U_i = Upper Boind of Inventory Level of station i

D_i = *Throughput* per hour of station i

T = Review Period (=20 hours)

Z = Z value of determined Service Level(*service level* 95%, $Z= 1.645$)

Tabu List & Aspiration Criteria

Initial Solution
Route A: 0-1-2
Route B: 0-3-4
Cost:100

M
O
V
E

Neighborhood Solution 1
Route A: 0-3-2
Route B: 0-1-4
Cost:90

Neighborhood Solution 2
Route A: 0-4-2
Route B: 0-3-1
Cost:85

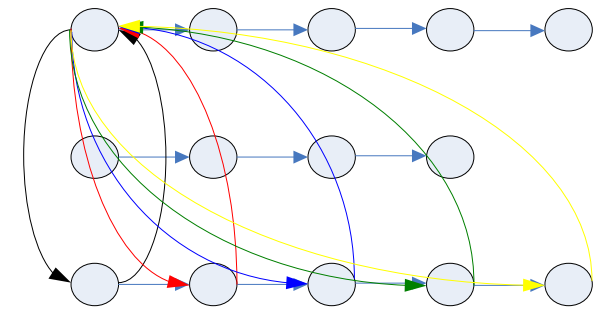
Neighborhood Solution 3
Route A: 0-1-3
Route B: 0-2-4
Cost:105

Neighborhood Solution 4
Route A: 0-1-4
Route B: 0-3-2
Cost:115

Iteration	Tabu Move
1	(4,RA,RB)&(1,RB,RA)
2	
...	
t+θ	

Tabu List

Tabu Length



Swapping

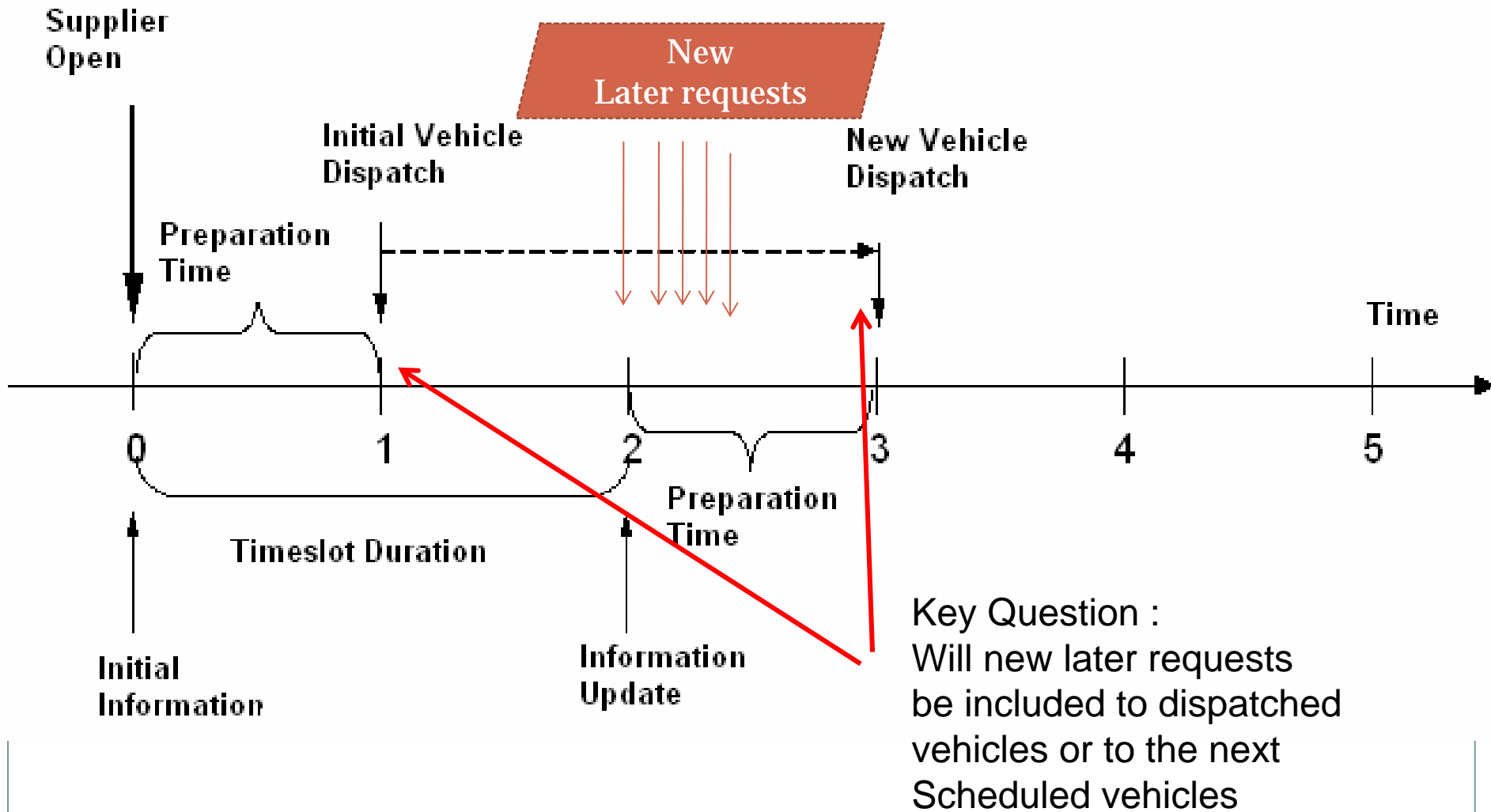
Static IIDP Static → Dynamic IIDP

Dynamic IIDP is a closed-loop system with retailer information updating as feedback (Inventory level in each retailer, position and the remain of capacity)



Dynamic IIDP can be viewed as repeated Static IIDP during the horizon planning

Time Frame of Dynamic Planning



Dynamic Mechanism



Information update

- The supplier updates the information based on timeslot given before. This information are inventory level, remaining capacity and position of vehicle that already dispatched.

New request handling

- After updates the information, the supplier recognizes new retailers that need to be delivered. Then it determines delivery quantities and delivery routes for these retailers.
- Suppose that old vehicle routes can not be inserted for the new request, so the supplier must generates new vehicle routes for the new retailers. This route generation conducted using nearest neighbor algorithm.

Synchronization between new and old routes

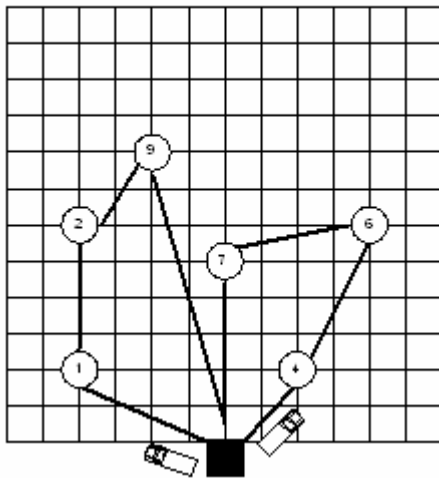
- Whenever it occurred new request and new routes have been constructed, synchronization can be made to minimize distribution cost while guarantee the service level for the retailer.
- We use tabu search algorithm.

Dynamic IIDP Model Description

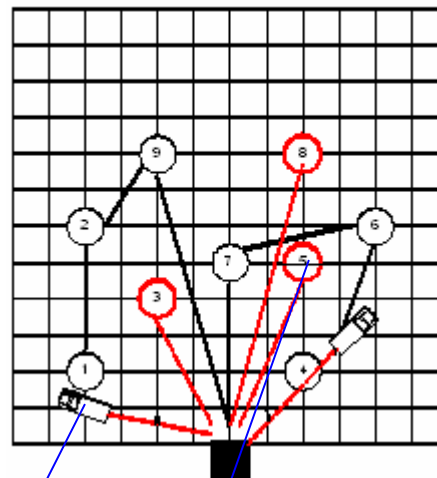
Static Condition

Dynamic Condition

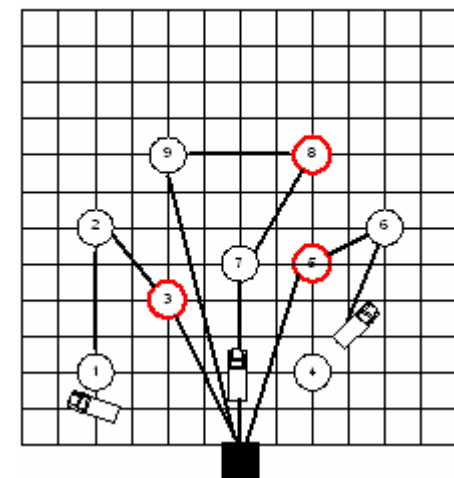
Initial Route...



Information Update...



Re-routing



Time

Vehicle position
and remaining load
at the truck

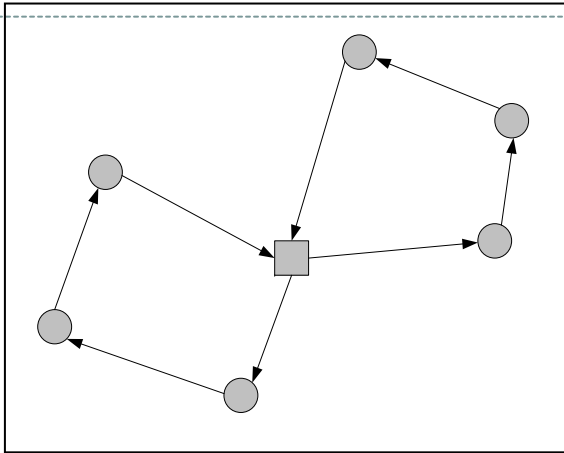
Inventory Level
of station i



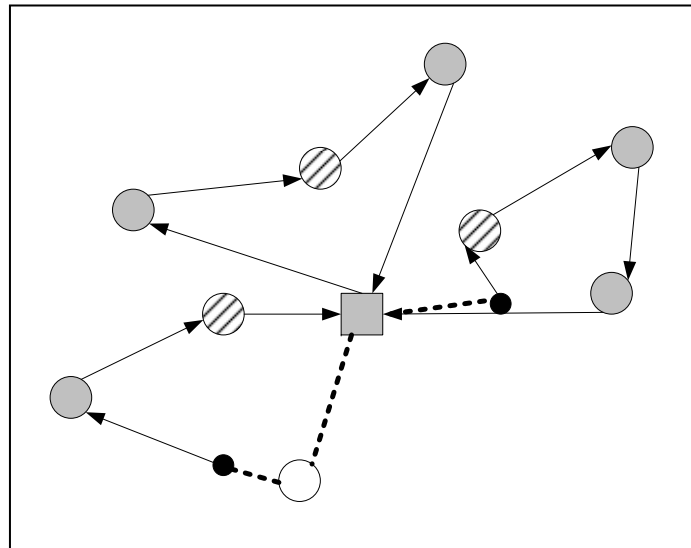
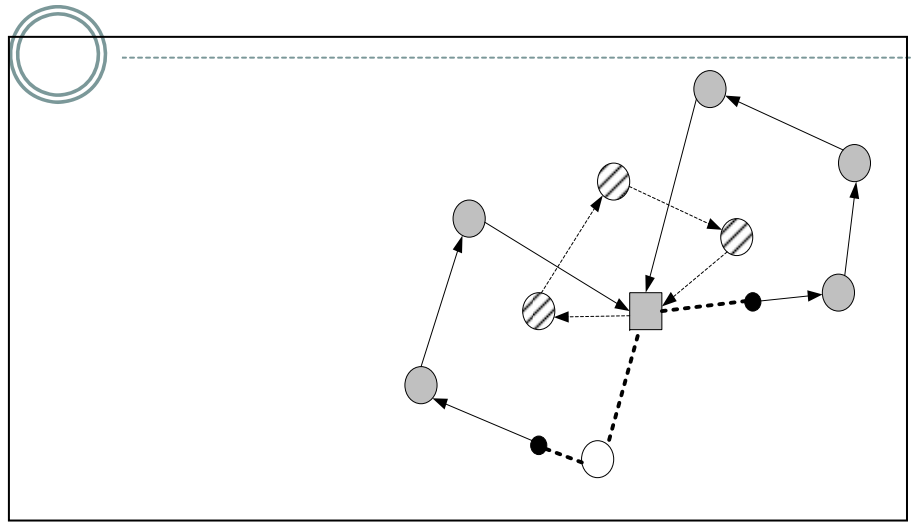
Supplier decides:

1. Delivery quantities
2. Delivery schedules
3. Delivery routes
4. Re-routing between new and old request

Updated Routes

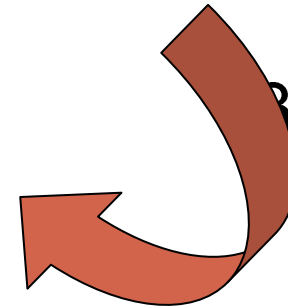


Initial Routes

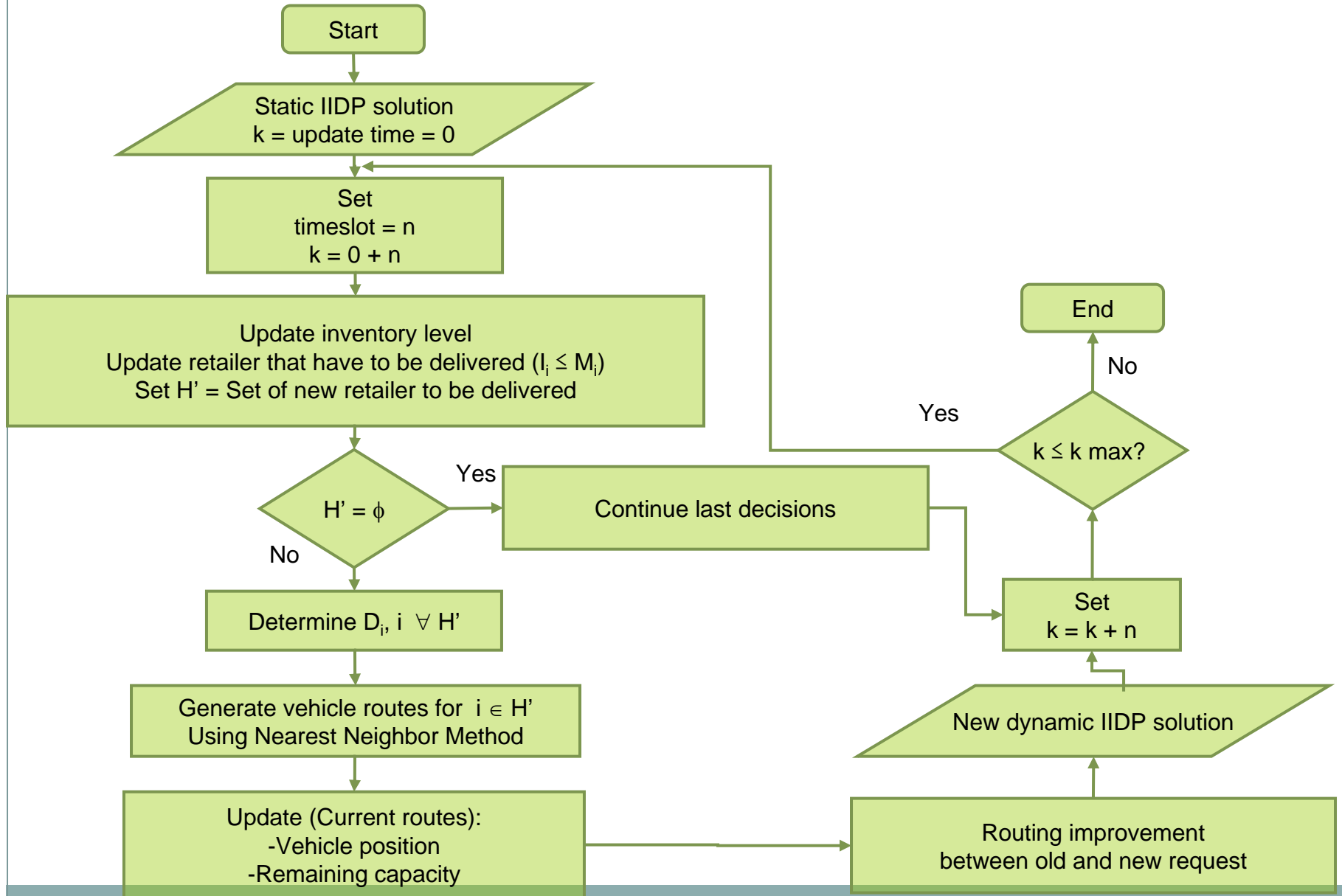


Updated Routes

Inserting New Requests



Dynamic IIDP: Flowchart



Prototye of Software

The software interface is titled "Dynamic Integrated Inventory and Distribution Problem" and is divided into several functional areas:

- Control Program:** Contains buttons for "Input Parameter" and "Reset Program".
- Routing Process:** Includes buttons for "Initial", "Graph", and "Save".
- Station Inventory Management:** Features buttons for "Delete", "Refresh", and "Upload Data li", along with a table of station data.
- Current Solution:** A table displaying routing details.
- Routing Process with Tabu Search:** Includes a checkbox for "Show Solution Every Iteration" and buttons for "Input", "Improve", "Graph", and "Save".

Five sections are highlighted with blue text annotations:

- Section 1:** Input Parameter
- Section 2:** Retailer Inventory Management
- Section 3:** Routing Initial
- Section 4:** Current Routing List
- Section 5:** Improvement Section

Computational Time: 0 MilliSecond

Station	Nomor SPBU	Alamat SPBU
0	0	0
4	54.601.01	JL.DUPAK RUKUN 72A-
5	54.601.02	JL.MULYOSARI NO.366
8	54.601.05	JL.TG.PRIOK(DP.LANTA
10	54.601.08	DS.TAMBAK LANGON 1
11	54.601.12	TAMBAK OSO SEMENI
16	54.601.19	JL.GRESIK 97
17	54.601.20	JL.GRESIK
18	54.601.21	JL.MARGOMULYO-TAN
19	54.601.23	JL.ANJASMORO 54
20	54.601.32	JL.SEMARANG NO.49
21	54.601.33	RAYA BALONGSARI N
23	54.601.35	JL.DARMO PERMAI TIM
24	54.601.36	JL.PRAPAT KURUNG
25	54.601.38	JL.ANGGREK 2 A SBY

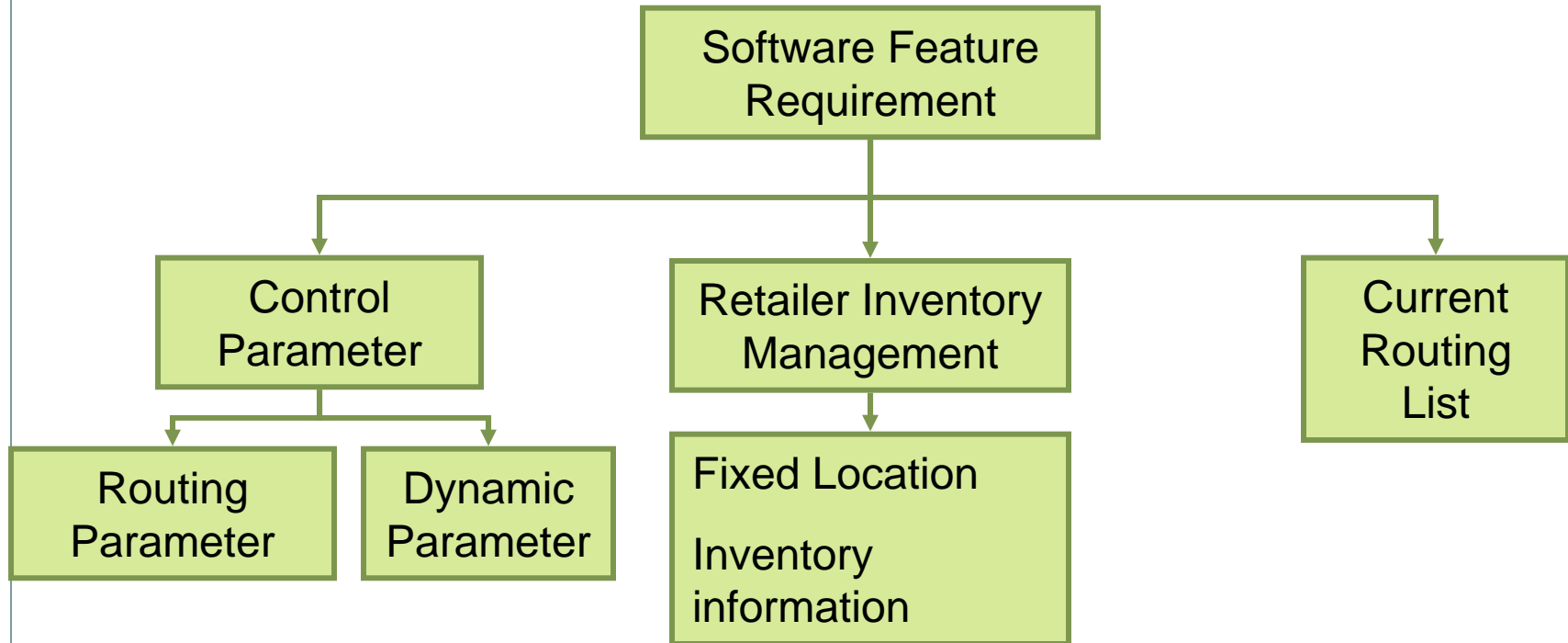
# Route	Route	Tot dist	Dist Cost	Trip Cost	Total Cost
*					

di di adjust

Show Solution Every Iteration

Input Improve
Graph Save

Software Features



Input Parameter

%fulfill	50
Vehicle Capacity	24
Vehicle Velocity	30
Max travel time	3
Service time	0.5
Cost per distance	885
Cost per Trip	12835.5

Set



Station Inventory Management

Delete Refresh Upload Data li



Updating data of Inventory Level

Initial Routes Development

and Distribution Problem

Routing Process

Initial Graph Save



Route Improvement

Setting Parameter Dynamic

<input type="checkbox"/> Min (%)	90
Iteration	10
Tabu Length (e)	2
Route	
Time Slot	2

Set



Routing Process with Tabu Search

Show Solution Every Iteration

Input Improve

Graph Save



Updating of Requests

Station Inventory Management

Delete Refresh Upload Data li



Conclusion

- We have developed a model and a heuristic algorithm for solving *Dynamic Integrated Inventory and Distribution Problem* (Dynamic IIDP) for A Gasoline Supply Chain
- The model is based on Vendor Managed Inventory Scheme where the supplier is responsible to the retailers' inventory.